# **Attributing Learned Concepts in Neural Networks to Training Data**

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# Why care?

Models seem to represent their important hidden features linearly as directions (the 'linear representation hypothesis').

We measure these *concepts* with linear probes, and ask the questions: 1. Which examples in the model's training data were important for learning these concepts?

2. *How robust is the formation of these concepts?* 

We approach this by **attributing concept probe predictions back to the base model's training set**.

We perform data attribution for learned hidden-layer concept directions.

Concept learning is convergent: robust to training example removal, and consistent across different training runs.

#### **Concepts of Interest**

• Snakes (ImageNet snake classes)







## Schematic of our approach for hidden feature attribution

#### Find concept directions for $f_{\leq i}$





1.Train *N* models with different random seeds on the training set.

2.Choose a hidden layer *i*, append a probing classifier *g* to its output, freeze the weights of  $g \circ f_{\leq i}$  on the concept dataset.

3.Calculate attributions (with e.g., TRAK) for  $g \circ f_{\leq i}$  on elements of the test set in terms of the original training data. Aggregate across fixed layers and concepts.

## Main Results

Training set attributions for concept learning

Robustness of concept learning



Concept presence at different network layers



to training exemplar removal concept: high-low frequency J. concept score for *X*<sub>*tr*, *j*</sub> 10 layer1.0.conv2 layer1 avg. ' attrib. s layer2 layer3  $10^1$   $10^2$   $10^3$   $10^4$  $10^{5}$  $10^{0}$ top-scoring training point index *i* J. concept score for  $X_{tr,i}$  $10_{-5}$  $10_{-2}$ concept: snakes layer1.0.conv2 layer1 avg. ( attrib. sc layer2  $10^{-8}$ laver3 10<sup>3</sup>  $10^{4}$  $10^{2}$ 10<sup>5</sup>  $10^{1}$  $10^{0}$ top-scoring training point index *i* concept: high-low frequency concept: snakes 1.01.0Т Т - 10000 - 10000 0.9 0.9 concept detection validation accuracy <sup>2.0</sup> <sup>2.0</sup> <sup>8.0</sup> 1000 1000 100 - 100 0.8 0.7 0.6 0.5 0.4 0.40.3  $10^{2}$ 10<sup>2</sup>  $10^{0}$  $10^{1}$  $10^{0}$  $10^{1}$ sparsity *k* sparsity k Top T concept-attributed training examples removed 12/6/23



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