The Intrinsic Manifolds of Radiological Images and their Role in Deep Learning

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Link to paper:

- The Manifold Hypothesis (MH): High dimensional data can be well described by a much smaller number of intrinsic dimensions.
 - Neural networks can learn to convert



Figure 1: Visualization of intrinsic lowdimensional image manifolds from [1].

Finding 2: Intrinsic Dimension and Generalization Ability

Generalization ability (GA) is sharply linearly correlated with dataset intrinsic dimension (ID) within radiological and natural imaging domains, but the steepness of this correlation differs noticeably between the two domains.

The slope of this GA vs. ID relationship is practically independent to model choice and/or training set size within an imaging domain.



data to abstract, informative features dimthat are *intrinsic* to the dataset.

- Why study the intrinsic dimension of medical images?
- Medical vs. natural images: different relevant semantics, yet we lack an understanding of how networks learn differently between the domains.
- Due to the MH, understanding the intrinsic structure of medical image datasets is key to analyzing how networks learn from them.

Objectives

- 1. Estimate the intrinsic dimensions of common radiology datasets, and compare to natural image datasets.
- 2. Evaluate the relationship of dataset intrinsic dimension with network generalization ability; comparing within and between the domains of radiological and natural images.

Estimating the Intrinsic Dimension of Image Manifolds

- ▶ By the MH: our *d*-dimensional data lies on a manifold $\mathcal{M} \subseteq \mathbb{R}^d$ such that $\dim \mathcal{M} = m \ll d$.
- We can estimate *m* via **maximum likelihood estimation**:

Figure 4: Linearity of model generalization ability with respect to dataset intrinsic dimension, for radiological and natural image datasets ($N_{\text{train}} = 2000$ on ResNet-18).

Experimental Settings

- Assume that the volume of \mathcal{M} scales exponentially with m as we move away from a point, and parameterize volume with k-NN distance T_k .
- ▶ Model data with a Poisson Process, and find *m* via MLE:



Datasets

► We analyze 7 common radiology datasets from different modalities:



Figure 2: Samples from our seven evaluated datasets.

Finding 1: Radiological vs. Natural Image Intrinsic Dimension

Radiological image datasets tend to have lower intrinsic dimension than

- Radiological vs. natural image IDs (Finding 1):
 - We estimated the ID of each dataset using 7500 images, evenly class-balanced according to a chosen binary classification task.
- **Generalization ability vs. ID (Finding 2):**
- We trained a network on each dataset for its respective binary classification task, and tested on 750 unseen data points.
- We evaluated 9 neural network models, each on 7 training set sizes, also performing task choice ablations.

Future Work

- Find theoretical support for the linear correlation of GA with dataset ID, and explain why the correlation sharpness differs between domains.
- Explore further uses of ID estimation for modeling, experimentation, etc.

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natural image datasets:



Figure 3: Intrinsic dimension of radiological and natural [2] image datasets.

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My website: https://nickk124.github.io/

References

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